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Structure Learning of Bayesian Network: A Review

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ABSTRACT

Machines using Bayesian networks can be used to construct the framework of information in artificial intelligence that connects the variables in a probabilistic way. "Deleting, reversing, moving, and inserting" is an approach to finding the best answer to the proposition of the problem in the algorithm. In the Enhanced Surface Water Searching Technique, most of the hunting for water is done by elephants during dry seasons. Pigeon Optimization, Simulated Annealing, Greedy Search, and the BDeu metrics

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Structure Learning, Global Search, Local Search, Pigeon Inspired Optimization.

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are being reviewed in combination to evaluate all these strategies being used to solve this problem. They subjected different data sets to the uncertainty matrix in an investigation to find out which of these approaches performed best. According to the evaluation data, the algorithm shows stronger results and delivers better points. Additionally, this article also represents the structure of the learning processes for Bayesian Networks as well.

1. Introduction

Biologists and social scientists build relational structures for their studies (Sun, X., Chen, C., Wang, L., Kang, H., Shen, Y., & Chen, Q. (2019)., 2019). But the network layout of a lot of nodes is very dense. Sometimes used in applied in statistics and machine learning, the probabilistic model is a random variable between an independent framework and a classification model, probabilistic networks are more often used to produce structure (Friedman, I. Nachman, and D. Peer,, 1999). Different models express the likelihood distributions in multidimensional space in different forms (Sun, X., Chen, C., Wang, L., Kang, H., Shen, Y., & Chen, Q. (2019)., 2019). A distinction in terms of structure and composition in the form of a probability distribution is used to differentiate between the two. A Bayesian model is more than just a reflection of information, it is a particular type of probability graph. When there are connections between different random variables, it will show interdependence (Xin, J., Chen, G., & Hai, Y , 2009). Although an acyclic structure is described as a random network between parameters (Friedman, I. Nachman, and D. Peer,, 1999), it can also be thought of as a guided acyclic graph. A Bayesian network has more often represented a multidimensional distribution or configuration of curves rather than arrows since it uses directional edges to express the probability distribution. " High-dimensional modeling will also cost a great deal of money to do. One approach to constructing network topology is by score, and the process is another route dependent on restrictions. It is difficult to create score functions, as well as check the optimization space. The primary advantage of the methodology based on restrictions is that it allows one to accurately determine whether a kind of freedom has been

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achieved. When learning is concerned with network optimization (KAREEM, S. & OKUR, M. C, 2017) (Friedman, I. Nachman, and D. Peer,, 1999), the best search approach is to use a scoring system that allows matching of the highest degree of structure on results (Yuan, C., Malonean, B., & Wu, X. , 2011). Based on the results of the variables being independent of each other, the network can find a way to create a Bayesian framework. So far, several clever Bayesian network layout learning algorithms have been suggested. This has well-clusters of observations (a frequently used Bayesian network built around LFO observations) (PC). Practical, feasible have various advantages and drawbacks, and thus, this algorithm has the potential to be used in a wide range of applications, such as in a mixed learning situation. "Compensate for network search space constraints with a learning algorithm, and recover Bayesian network score from sparse graphs" (CIBNS). Using the Bayesian network to help, and the data that was given as an example above can cut down on the blindness of the quest (Djan-Sampson, P. O., & Sahin, F. , 2004). As a result, a combination of constraint-action and search-based methods will further increase the performance of Bayesian network research (Syah, et al., 2021). At the same time, it's good for finding the global optimum. Since the relationships of random variables can be represented with direct acyclic graphs (DAGs) and are therefore useful in realms such as artificial intelligence, medicine, bioinformatics, and sociology, they have been widely applied in the economy, as well. The framework learning mechanism has gained popularity in recent years and is now almost ubiquitous (Yang, 2010). With regards to learning the structures of DAGs from evidence, two methods have predominated: As well, the quest and restriction methods and mixed methods have been used. Rebuilding DAGs Conditional approaches for determining BN structure, such as the use of independence measures as well as search-based methods, have been suggested (Yang, 2010). Constraint-based methods construct using variables that have conditional independence (correlation) dependent on each other. He uses IC, PC, and TPDA (three-oriented dependency analysis) in this class. A score-based search is used to discover the network's ideal setup under which search constraints are applied only to the superstructure of the graph. A reduction in the search space will result in better solutions (Djan-Sampson, P. O., & Sahin, F. , 2004). Verma and Pearl gave an IC which looks for all subsets of u and v, for the assumption that no

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subsets of the two variables are conditionally dependent on some other subset of variables and that all other subsets are independent of that subset of the whole, and which partitions S into u and v are mutually exclusive and which are mutually nonexclusive. This procedure was suggested by Spirtes and Glymour, an iterative way of looking for the cardinality of increasing subsets of items was ((Shahab Wahhab Kareem, Mehmet Cudi Okur, 2020) (Shahab Wahhab Kareem, Mehmet Cudi Okur, 2019) (Shahab Kareem, Mehmet C Okur, 2018)). The PC algorithm constrains the set of vertices that may separate U and V to vertices that are either directly connected or that are adjacent to V (Zhang, Y., Liu, J., & Liu, Y, 2018). As the number of vertices in a DAG expands, the asymptotic consistency of the algorithm remains intact.

2. Related Works

2.1. Bayesian Network

Because of their capacity to deal with non-deterministic variables in the physical universe (Friedman, I. Nachman, and D. Peer,, 1999), probabilistic models have been widely used in recent years. The joint probability distribution of random variables can be defined by a Bayesian network (Bayesian) network (BN) (Cowie, J., Oteniya, L., & Coles, R., 2007). A Bayesian network is a graph in which variables are represented by nodes and Bayesian probabilities are described (Shahab Wahhab Kareem and Mehmet Cudi Okur, 2020). Structure learning is based on the idea that learning is just a form of parameter learning. The likelihood is obtained for each variable probabilistically for those variables it has to have (Zhang, Y., Liu, J., & Liu, Y, 2018). It detects a DAG with one node for each variable in the structure. Variables used in the system are conditionally independent of their non-descendants about their values, whether the conditions specified are not true for any of the nodes lower in the network (Cowie, J., Oteniya, L., & Coles, R., 2007). Lately, extensive research has been conducted on discovering how BNs work based on actual evidence. Learned dependency graph analysis may be valuable in helping to define the problem and is also utilized in solving it (Cowie, J., Oteniya, L., & Coles, R., 2007). The Cooper-Herskovitzler k2 algorithm was first suggested in 1992, and virtual annealing BN was improved in 1995 (SA). Larranaga in 1996, used a genetic algorithm (GA) to apply it to the design of neural network structures.

A Bayesian network S = {G, θ} for a series of n quantities that expresses the conditional probability mass function of its constituent variables, and θ is defined by a guided acyclic graph X = {X1, X 2,..., X n} etc.

$$p(G \mid D) \propto p(G)\, p(D|G) \qquad (1)$$

In the Bayesian network, G, a correlation between two variables implies that they are interconnected and an edge occurs. If the structure G is valid, then it means that before seeing some data, the prior data holds. It is conditional on the probability. To treat P (G and D) as a ranking (Wang, J., & Liu, S. , 2018), one can use a heuristic search algorithm. One can search for a high-scoring network. For example, a greedy search of the area in question, looking at all nearby structures, calculates the score and goes to the structure with the best score. It ends because the new arrangement is greater than any of the surrounding structures. Hence, computing a network structure can be described as an optimization problem (Tong, S., & Koller, D. , 2001), where the objective is to find the best possible quality for the training data. It can be done using a Bayesian method, a minimal knowledge criterion, or a combination of the two. These measurements may be applied to entire networks, and their results summarized as a (or composed) as the total (or product) of their parts. It's easier to score and therefore to locate when it's done locally. If you are looking for familiarity, K2, HillClimber, SA, and GA are good ways to go. Probabilistic models, because of their power to describe uncertain information, are often highly effective aids. Probability theory offers an analysis method for determining how the elements are linked together to ensure the system's consistency. There is supposed to be little overlap between the two sets of findings, and different approaches are necessary to come up with new models for the data. Graph theory provides an intuitive general-purpose interface for creating arrays of interactional (Li, J., & Chen, J. , 2014), variable-structure data that can be used in varied algorithms. Maybe 'probabilistic graphical simulations' may be referred to as Bayesian networks (Cooper, G. F., & Yoo, C., 1999). While probabilistic networks are a more complex and more flexible technique, Bayesian networks (BN) can be considered a simpler analytical approach for machine learning (Kareem, 2020) (Cooper G F, Herskovits E, 1992). They can be applied through information development, discourse, and derivation. The Bayesian network

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had the following structure: DAGs with two critical nodes. A variety of the network is created by the parameters and its overall configuration. This structure describes parameter dependencies, and these parameters represent conditional probabilities (Zhang, Y., Liu, J., & Liu, Y, 2018). Without an effective search tool, building a Bayesian network is a challenge. Given a dataset, the optimization problem of finding the optimum configuration of a Bayesian network (BN) is NP-complete (Kareem, S. W., & Okur, M. C, 2019). Although significant research to come up with an approximation of network structures has been done, In essence, there are two approaches to structural learning in Bayesian networks. While the first use constraint-based techniques (Silva L. A. Bezzera J. B. Perkusich M. B. Gorgônio K. C. Almeida H. O. Perkusich A., 2019), and searches, the second employs a method that utilizes scoring and searching techniques. A calculation is used to find the BN composition.

2.2. Structure Learning of Bayesian Network

A probabilistic paradigm incorporates mathematics, as well as graphical representations of concepts that were developed by graph theory (Tahier, T., Marie, S., Girard, S., & Forbes, F. , 2019). Two problems must be addressed: ambiguity and unpredictability. Graphical models are joint probabilistic systems that depict random dependency relationships Algorithms provide a large impact in analyzing and in the design and development of machine learning approaches Diagrammatic models use probabilities, where nodes represent random variables and/or association between pairs of variables may be drawn to display relationships. compressed mutual likelihood distributions There are two essential kinds of software programs: writer-prompts and reader-prompts (Cooper, G. F., & Yoo, C., 1999). Markov Random Fields (MRFs) or Bayesian Networks may also be classified as undirected models. Observational learning has been researched throughout the latest decade. The use of experience or observed evidence can be used to generate new principles (Tong, S., & Koller, D. , 2001). Although there has been some study on this topic, different approaches have been tried to Make just the changes to the data necessary to reconstruct the feature (Cooper, G. F., & Yoo, C., 1999). To change the whole graph to optimize a ranking, but the alterations could create dependencies. Optimization techniques aim to create a local version of the network to better approximate the

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global structure. Most analysis with Bayesian networks is limited to scenarios in which the configuration does not change. Traditional algorithms also used scores were used for the bulk of these algorithms (P. Larranaga, M. Poza, Y. Yurramendi, R. H. Murga and C. M. H. Kuijpers, 1994) it may determine the likelihood of all DAG models if there are just a few random variables, including all possibilities (Li, J., & Chen, J. , 2014).

$$f(n) = \sum_{i=1}^{n} (-1)^{i+1} \binom{n}{i} 2^{i(n-i)} f(n-i) \text{ n>2} \qquad (2)$$

Where, f(0) = 1, f(1) = 1.

But for all practical purposes, this amount should be huge. Checkering has shown that for certain groups of DAG patterns that this is so. Using smarter search algorithms may help solve this sort of issue. For example, authors will select values of a stochastic variable (SV) that increase the probability of obtaining p (Note that there should be higher than one maximizing model.) As the number of variables grows, finding the optimal models among all possible models becomes infeasible to the method.

2.3. Pigeon Inspired Optimization

Currently, the majority of Pigeon-inspired optimization (PIO) has been used in continuous optimization problems. as the follow-up from problem orientation: the Metropolis adoption of simulated annealing is suggested as a solution to this discrete PI-O (DPIO) algorithm; (TSPs).

$$Vi(t) = Vi(t-1).e^{-Rt} + \text{rand.(Pg-Pi(t-1))} \qquad (3)$$

$$Pi(t) = Pi(t-1) + Vi(t) \qquad (4)$$

DPIO is developing a new chart and compass that will make it easier for explorers to understand and advance. a modern hallmark operator, which is intended to increase the performance of TSPs using cooperative learning and heuristic knowledge. The Metropolis approval criteria are used to determine if new solutions should be allowed to converge or not, particularly if they are otherwise trying to be effective (Kulkarni, A. J., Krishasamy, G., & Abraham, A. . , 2017). Experiments were carried out to observe

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the behavior of the map and compass operator as well as other landmark workers and learn their differences.

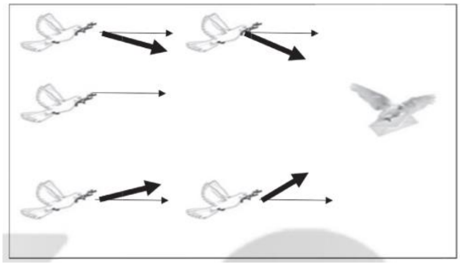

Figure 1. Compass operator and map for PIO.

Pigeon Inspired Optimization is a method is a novel bio-inspired optimization method In terms of pigeons (Cao, M. Raoof, E. Szabo, J. Ottosson, and I. Näslund, , 2020), it was on the first account that the navigational methodology was created, and in air-vehicle applications, it was later.

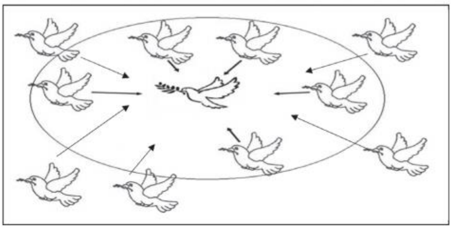

Figure2. Landmark operator model for PIO.

Any PIO has two essential-valued components: a mapping driver and a way-finder, and a geographic/direction driver, and another that values landmarks. In the map and compass domain driver, there are many suns, while in the landmark driver, there are just a few landmarks (Kulkarni, A. J., Krishasamy, G., & Abraham, A. . , 2017). In layered form, it mimics the aptitude of handyman do vessel pigeons during the map and compass, each team member learns new navigation techniques, including D-dimensional explorations. They will get to know a new position and velocity IP and velocity I by each one of our techniques. Many the pigeons can locate their targets because of the magnetic field. They often use landmarks to figure out where they are.

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The suggested solution utilizes a Bayesian search using a PIO search tool (Cheng J, Grainer G, Kelly J, et al. , 2001). To calculate the Bayesian network configuration, the BDeu metric was used. Any pigeon in the population encodes a location and velocity in the specified room (Koski, T., & Noble, J. M., 2009). This place is believed to be the optimal search location. It is focused on two methods. For the first technique, the local quest procedure is navigated using a schematic of a globe and compass. Second, it employs a landmark paradigm for a worldwide quest (Cheng J, Grainer G, Kelly J, et al. , 2001). The pseudo-code of this algorithm is seen in Figure 3. PIO algorithm may include the use of various neighborhood-specific search algorithms. When searching for solutions created by pigeons (Lam W, Bacchus F, , 199), you can depend on being up-to-to-date. The DAGs for studying BRTs are a part of the solution space to be investigated. Any pigeon represents a solution and is started on an empty seed DAG (Khanteymoori, A., Olayee, M. H., Abbaszadeh, O., & Valian, M. , 2018). When the pigeon is looking for a likely network layout, defined as the BDeu metric, it explores inside the quest room. Equation 4 seeks to find the network with the greatest BDeu score.

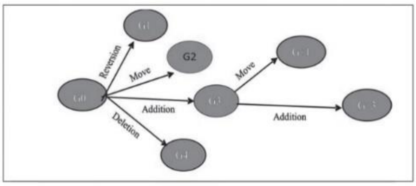

Figure 3. Compass steps for a particular pigeon.

At any turn, new ideas are developed through trial and error. If you start with an empty graph, all arcs will be appended. The process is repeated until the specified number of arcs has been created. As a result, each operator is initialized with the initial population and the one that raises the BDeu score is chosen (Bartlett and J. Cussens, 2017). As long as BDeu or as long as necessary, the operator sees an improvement, the pigeon can keep flying (Salama, K. M., & Freitas, A. A., 2012; Salama, K. M., & Freitas, A. A., 2012). Operators usually are called the four basic optimization operators: addition, elimination, movement, and mutation, and replacement. It is an uncomplicated set up in this particular domain and only replaces

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one competitor edge per time (Spirtes, C. Glymour, and R. Scheines, 2001; Spirtes, C. Glymour, and R. Scheines, 2001), with the four operators working around the board. On the other side, moving the solution about in some medium affects it, in a mild manner (Liu F, Tian F, Zhu Q. (2007)., 2007; Liu F, Tian F, Zhu Q. (2007)., 2007). Correcting a solution without the three basic operators would not automatically result in a better solution (Bartlett and J. Cussens, 2017). Higher ground-hopping occurs with proximity to a sought-after destination. Moving the cursor to a lot about is referred to as pigeon-skipping in literature. Landmark is a complex and interesting combination of traveling and seeking. A DAG defines a pigeon as one which does revert, moves, makes new arcs, and ads, and reaches solutions G1, G2, G3, and G4 in succession (Sencer, S., Oztemel, E., Taskin, H., & Torkul, O., 2013; Sencer, S., Oztemel, E., Taskin, H., & Torkul, O., 2013). As suggested by G3, then considering the BDeu score, it will look for another operator that satisfies G3 If the BDeu (behavioral + economics) score of G+1 is greater than that of G then it can carry out the associated action.

3. Methodology

Using the positivist philosophical approach, this research targets to maintain the development of knowledge to assess the outcomes. In this process, gradual management of the information and process simulation is necessary. For the comparative analysis of the literature, several determiners such as AND, OR, BUT, etc. have been used for the keywords such as Bayesian network, structure processing, structure learning, conditional independence test, etc.

To simulate the comparative review, articles have been collected from reliable journals. Articles published from 2010 to 2020 have been chosen for the comparative review because of the scarcity of quality journals. A systematic comparison among the selected articles will be conducted in this review. Comparative analyses have been conducted based on available articles in this regard.

4. Analysis and Findings

4.1. literature survey

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Table 1. literature survey for each cited paper and what they founded

Authors	Findings
(Aouay, S., Jamoussi, S., & Ben Ayed, Y. , 2013; Wang, J., & Liu, S. , 2018)	A bi-velocity discrete particle swarm optimization with mutation operators is presented to train Bayesian networks. Mutation in the suggested method can effectively avoid premature convergence and boost the population's exploration capabilities. Using data from three well-known benchmark networks, the authors compare the proposed approach to alternative algorithms. Experiment findings show that the suggested algorithm is better at learning Bayesian networks than any other currently available method. Binary strings representing a directed acyclic network are encoded and assessed using the K2 metric for each swarm particle. Updates in velocity and location are made for every particle throughout the iteration.
(Long, 2016)	The paper proposes a hybrid algorithm that they term a Bayesian network model-based conditional independence test and a heuristic scan (CIBNS, CI-based Bayesian Network Search). To ensure the solution consistency and search speed, the latest algorithm initially uses the conditional independence test to compact the search space. After that, the algorithm implements a heuristic search method that incorporates the BDeu Measure score to boost performance in the construction process. On simulated and actual info, the latest algorithm finds that it is capable of efficiently constructing a network for aviation. It outclasses hill climbing and local hunt in terms of utility and precision.
(Cao, M. Raoof, E. Szabo, J. Ottosson, and I. Näslund, , 2020)	The authors apply the falcon optimization algorithm (FOA) to the learning structure of a Bayesian network. This paper has employed reversing, deleting, moving, and inserting to obtain the FOA for approaching the optimal solution of a structure. Essentially, the falcon prey search strategy is used in the FOA algorithm. The result of the proposed technique is associated with pigeon-inspired optimization, greedy search, and simulated annealing that apply the BDeu score function. The authors have also examined the performances of the confusion matrix of these techniques by utilizing several benchmark data sets. As shown by the experimental evaluations, the proposed method has a more reliable performance than other algorithms (including the production of excellent scores and accuracy values).
(Li, J., & Zhang, Y., 2014; Talvitie & Koivisto, 2019)	local scores based on classification and regression trees are introduced. It is possible to discover a tree structure that maximizes a Bayes score for a variety of medium-sized issue cases with minor limits on the tree structure's available branchings. Thus, the Bayesian network structure may be optimized globally, including the local structure. A similar model class is also introduced that extends conventional conditional probability tables to continuous variables by applying an adaptive discretization method. Empirical comparisons between the two groups of models are made by the construction of Bayesian networks based on real-world and synthetic data. According to their structure learning capacity,

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	prediction performance, and running duration, the model classes have different strengths.
(Shahab Kareem, Mehmet C Okur, 2018; Shahab Kareem, Mehmet C Okur, 2018)	The authors regarded Bayesian networks structure learning as widely considered to be a difficult computational problem, as the more candidate graphs you have, the more the ratio of variables grows exponentially. There have been several heuristic searching techniques that attempt to improve network layout. they demonstrate two methods for enhancing Bayesian network layout learning using search optimization in this article. This method combines elements of Greedy quest with elements of Bee optimization algorithms. To test this suggested strategy, they are going to use two search techniques.
(Cheng, S., & Shi, Y. (Eds.)., 2020; Cheng, S., & Shi, Y. (Eds.)., 2020)	Using Bayesian networks, machine learning experts may construct a framework for information that depicts the probability relationship between variables. Elephant Swarm Water Search Algorithm (ESWSA) was introduced as a new way to build Bayesian networks. The algorithms involved include the ones mentioned below: Deleting, Reversing, Inserting, and Moving are both used to arrive at the optimum solution structure with the ESWSA. Mostly, elephants' use of water quest technique during droughts is incorporated into the ESWSA algorithm. To assess all algorithms, BDeu (Bird-inspired Efficient) score function is used. They compared the confusion matrix performances of these methods with different data sets to get a better understanding of them. The findings of the evaluations show that the algorithm suggested does better than the other algorithms, both in terms of efficiency and results.

Table 2. Comparison of the Methods for structure learning Bayesian network

References	Data	Algorithms	Results			
(Wang, J., & Liu, S. , 2018)		BVD-MPSO-BN	Node	HKS	LKS	AKS
			500	-2527.9	-2554.9	-2536.6
	ALARM		1000	-5032.2	5054.9	-5038.4
			2000	-9721.8	-9727.2	-9723.1
			500	-555.2	-555.2	-555.2
	Asia,		1000	-1100.8	-1101.4	-1100.8
			3000	-3325.9	-3326.3	-3326.0
			500	-2707.3	-2716.5	-2709.9
	Credit		1000	-533.9	-5338.7	-5335.9
			3000	-15806.2	-15808.4	-15806.4

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(Long, 2016)	ALARM	CIBNS , TPDA and PC	Node 100 200 300 400 500	CIBNS 0.86 2.31 6.92 16.83 83.29	TPDA 0.89 2.98 9.93 21.16 101.63	PC 1.94 5.67 14.69 95.87 568.43
(Talvitie & Koivisto, 2019)		Intersection-Validation PCARTp vs FTP	Sample size 1/64 1/32	Win 21 26	Tie 30 24	Loss 1 2
(Cheng, S., & Shi, Y. (Eds.)., 2020)	ALARM, ANDES	ESWSA	BDeu -160095 - 469217	Accuracy 75% 60%	F1Score 0.85 0.68	AHD 0.45 0.45
(Kareem S. O., 2021)	Hepar, Adult	FOA	BDeu -160,055 -20,535	Accuracy 73% 58%	F1Score 0.75 0.52	AHD 0.28 0.45

4.2. Analysis of Findings

Through developing theories of ambiguity reasoning in the 1980s, Bayesian networks (or Bayesian belief networks) have come to the forefront of artificial intelligence science. recently, BNs are an important method in dealing with unpredictable systems and data processing of multivariate random variables Determining the network configuration and parameters with datasets derived from previous analyses (Yang, C., Ji, J., Liu, J., Liu, J., & Yin, B. , 2016; Yang, C., Ji, J., Liu, J., Liu, J., & Yin, B. , 2016). Structure or parameter learning into two parts: structure learning and parameter identification. In the former, the network topology determination involves identifying the topologically suitable sample sets. The details of the network topology are needed to establish the network parameters (Kh., 2020). Bayesian learning also involves access to network topology and data, making it the foundation of Bayesian network growth. A good way to find the 'optimization structure' is to be based on identifying effective structural principles. There are two models of Bayesian Networks, which could be derived from a Bayesian framework learning process, as a way of breaking down a Bayesian inference system, the DAG method may be considered a graph that codifies the interdependence between variables (Zhang, Y., Liu, J., & Liu, Y, 2018; Zhang, Y., Liu, J., & Liu, Y, 2018). conditional freedom is confirmed by experimentation. Stress on relevancy approaches Once you have chosen a quest strategy, the best network will be found (Zhang, Y., Liu, J., & Liu, Y, 2018; Zhang, Y., Liu, J., & Liu, Y, 2018). There are means of assessing how accurately can classify participants (commoner ones include maximum probability, Bayesian Information Criterion, (Ashish Sharma, 2022) (Al-Alkawi, H. J. M., Hanfesh, A. O., & Mohammed Rauof, S. M. N., 2019) (M. K. Hasan, M. M. Islam, and M. Hashem, , 2016) (M.V. Prakash, V. Porkodi, S. Rajanarayanan, M. Khan, B.F. Ibrahim, M. Sivaram, 2020) (Qasim, A.J., Din, R.E., Alyousuf, F.Q.A, 2020) (Xiao-guang Gao, Zhi-Gao Guo, Hao Ren, Yu Yang, Da-qing Chen, Chu-Chao He, 2019) Bayesian ranking, and Minimum Description Length), as well as uncommon means (Maximum Product-Likelihood, Bayesian Information, and Minimum Description). Searching for the most optimal network is an intractable challenge and refined algorithms are almost impossible to implement (Zhang, Y., Liu, J., & Liu, Y, 2018; Zhang, Y., Liu, J., & Liu, Y, 2018). Manually controlled approaches have included techniques, such as Greedy hill-climbing (Xiao-guang Gao, Zhi-Gao Guo, Hao Ren, Yu Yang, Da-qing Chen, Chu-Chao He, 2019), Simulated Annealing, Evolutionary Algorithm (EA), and Genetic Algorithm (GA). GA and EA have been widely employed. Because the number of variables is high, both of the above algorithms are likely to return a local optimized network structure until convergence is reached (Andrews, J. Ramsey, and G. F. Cooper, 2018). In this paper, a novel approach focused on a new-to-discrete Particle-Behavioural Quantum algorithm (NDPB) is used to learn BNs' structure Statistical dependencies are easy to express in a Bayesian network (BN). It harnesses the power of graph theory to represent random variables' Dynamic Bayesian Networks (DBNs) is a type of Bayesian Networks (BNs) which deals with time-varying processes. Due to DBN's ability to describe nonlinear, time-dependent, changing, and probabilistic relationships, much of DBN learning and modeling research has emerged. DBNs have also been employed in many different sectors. Many complex Bayesian networks are built by asking a professional for help. When working for smaller networks, elicitation may be

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straightforward, but when doing so for huge numbers of variables, it becomes cumbersome and time-consuming. If information is accessible, it is feasible to construct the model on that (Andrews, J. Ramsey, and G. F. Cooper, 2018). If all the data have been collected, studying two networks can be modeled when the complex Bayesian network results in the expression of a prior network and transformation network since the fitness mechanism is a closed-form (Andrews, J. Ramsey, and G. F. Cooper, 2018). Data normally include errors, because typically cannot accurately observe the mechanism the authors are trying to represent. An additional difficulty with missing data is that it operates as a closed-form with comprehensive data, though not limited to that. What's needed for learning a database structure from incomplete data is entirely is much more effort than what's required for a well-structured database (Shahab Wahhab Kareem, Mehmet Cudi Okur, 2019), from 1998 onward, the use of DBN (Structural EM), can be seen in latent variable models. Deterministic approaches, on the other hand, are vulnerable to finding local optima, are said to be weak at generalizing, and may be wide in their quest space (Shahab Wahhab Kareem, Mehmet Cudi Okur, 2019). When a local maximum has been reached, an easy solution to the problem is to use a stochastic approach this paper introduces complex Bayesian networks using particle swarm optimization (PSO) (He, C.-C., & Gao, X.-G, 2018, July 25-27). The authors choose that as a result of the job. Since networks can be viewed as components, authors can develop more complex systems by sharing their parts with higher fitness.

5. Conclusion

Using the Pigeon-Inspired Learning method, the authors concentrated on the structure learning issue and applied it to the Bayesian network. They are useful for the design of information representation systems in machine learning. It is possible to encode probabilistic dependencies among the variables using Bayesian networks (Xingping Sun, Chang Chen, Lu Wang, Hongwei Kang, Yong Shen, and Qingyi Chen, 2019). Scoring and scanning is one layout learning methodology at Bay Networks. Propose a new Bayesian network framework based on PIO (PIO). It's a basic concentration rate (Xiao-guang Gao, Zhi-Gao Guo, Hao Ren, Yu Yang, Da-qing Chen, Chu-Chao He, 2019). An unbelievable and remarkable navigational skill can be seen in pigeons in the way they just seem to find their way a guided acyclic graph Any chart has a fitness score that tells its ability to demonstrate this reality. The algorithm takes time to explore the solution space (Zhang, Y., Liu, J., & Liu, Y, 2018; Zhang, Y., Liu, J., & Liu, Y, 2018), so it is performed using a landmark, compass, and map operator before it achieves the best or a suitable structure is found. When implementing the suggested approach, simulated annealing and greedy search were contrasted with each other with the BDeu value (Gao, T., & Wei, D. , 2018). In addition, the authors tested the uncertainty approaches in a variety of data sets. A specific algorithm yields outstanding results as shown by the effects produced it produces better results, is as effective, and produces higher and better values than simulated annealing and greedy algorithms (Kareem, S. W., & Okur, M. C, 2019; Kareem, S. W., & Okur, M. C, 2019). The authors used the score and search method, where PI is a parameter and the search tool. a search strategy that uses the random flights of a pigeon as its basis (Gao, T., & Wei, D. , 2018). The hunt seems to follow the path of least resistance, so PIO is a popular technique for finding discrete solutions. Easily tailored to a specific to every target area. Prompting PIO exploration results in a likely-to-be-tried solution because allowing pigeons to travel in short-range leads to plausible solutions by parameter input. According to the suggested approach (Zhang, Y., Liu, J., & Liu, Y, 2018), the structure of the network, it is capable of finding outstanding structure solutions, which means it can measure better function and approximates more accurately. The algorithms make the quest faster and convergence is rapid. The suggested solution may be studied as a study in parallel processing.

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فێربوونی پێکهاتەی تۆڕی بیزی بە بەکارهێنانی لۆگاریتمی زیرەکی سوێرم: پێداچوونەوەیەک

پـوختـە:

ئەو ئامێرانەی کە تۆڕەکانی بیزیان بەکاردەهێنن دەتوانرێت بەکاربهێنرێن بۆ دروستکردنی چوارچێوەی زانیاری لە زیرەکی دەستکرددا کە بە شێوەیەکی بایبەتی بە گۆڕێنەرەکانەوە گرێ دەدات. "سڕینەوە، پێچەوانەکردنەوە، جوڵاندن، و داخڵکردن" ڕێبازێکە بۆ دۆزینەوەی باشترین وەڵام بۆ سەلمێنەری کێشەکە لە لۆگاریتمەکەدا. لە تەکنیکی گەڕانی ئاوی ڕووکەشی پێشکەوتوودا، بەزۆری، ڕاوکردن بۆ ئاو لە ماوەی وەرزی وشکدا لەلایەن فیلەکانەوە ئەنجام دەدرێت، ئەوە بەگەڕخستنی کۆترییە، شیکاریی و گەڕانی چاوچنۆک و پێوەری BDeu بە تێکەڵی پێداچونەوەی بۆ هەڵسەنگاندنی هەموو ئەو ستراتیژیانە ئەوان کۆمەڵێک داتای جیاوازیان کرد بۆ ماتریسی نادڵنیایی لە لێکۆڵینەوەیەکدا بۆ زانینی ئەوەی کام لەم ڕێبازانە باشترینیان ئەنجام داوە. بەپێی داتای هەڵسەنگاندن، لۆگاریتمەکە ئەنجامی بەهێزتر پیشان دەدات و خاڵی باشتر دەگەیەنێت. هەروەها، ئەم وتارە هەروەها نوێنەرایەتی پرۆسەی فێربوونی پێکهاتە دەکات بۆ تۆڕی بیزیان هەروەها.

التعلم الهيكلي لشبكة بايز باستخدام خوارزمية سرب الذكية: مراجعة

الملخص:

يمكن استخدام الآلات التي تستخدم شبكات Bayesian لبناء إطار عمل للمعلومات في الذكاء الاصطناعي يربط المتغيرات بطريقة احتمالية. يعد "الحذف ، والعكس ، والتحريك ، والإدراج" طريقة لإيجاد أفضل إجابة لاقتراح المشكلة في الخوارزمية. في تقنية البحث عن المياه السطحية المحسنة ، في الغالب ، يتم البحث عن المياه بواسطة الأفيال خلال المواسم الجافة ، وهو تحسين الحمام ، والتلدين المحاكي ، والبحث الجشع ، ومقاييس BDeu التي يتم مراجعتها معًا لتقييم كل هذه الاستراتيجيات المستخدمة بالترتيب لحل هذه المشكلة. لقد أخضعوا مجموعات بيانات مختلفة لمصفوفة عدم اليقين في التحقيق لمعرفة أي من هذه الأساليب كان الأفضل أداءً. وفقًا لبيانات التقييم ، تُظهر الخوارزمية نتائج أقوى وتقدم نقاطًا أفضل. بالإضافة إلى ذلك ، تمثل هذه المقالة أيضًا عمليات التعلم الهيكلية لشبكة Bayesian Network أيضًا.